

1-loop integrals and the Feynman parametrization

Exercise 1: Many loop integrals can be simplified with the so-called Feynman parametrization. Its starting point is the identity

$$\frac{1}{ab} = \int_0^1 \frac{dt}{[at + b(1-t)]^2}, \quad a, b > 0.$$

Verify the validity of this relation.

Exercise 2: We consider the integral

$$B(Q^2; m^2, m^2) \equiv \int \frac{d^d P}{(2\pi)^d} \frac{1}{P^2 + m^2} \frac{1}{(P + Q)^2 + m^2}.$$

- (a) Argue that the result only depends on the length squared $Q^2 = \sum_{\mu} Q_{\mu} Q_{\mu}$, rather than the individual components of the vector Q .
- (b) Show examples of Feynman diagrams that would lead to this integral.
- (c) After inserting $d = 4 - 2\epsilon$, make use of the Feynman parametrization and the results in exercise 12.2, in order to determine $B(Q^2; m^2, m^2)$ up to order ϵ^0 .